

# Heavy fermions and superconductivity in the periodic Anderson-Holstein model

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Recent discovery of rattling motions in the filled skutterdites such as  $\text{PrOs}_4\text{Sb}_{12}$  [1] and the clathrates such as  $\text{Ce}_3\text{Pa}_{20}\text{Ge}_6$  [2] has stimulated much interest in the strong coupling of Einstein phonons to electrons in heavy-fermion systems. The simplest realization of such systems is the periodic Anderson-Holstein model where the Einstein phonons at each site couple to the local ( $f$ -) electrons which hybridize with the conduction electrons. We study this model on the basis of the dynamical mean-field theory in which the effective impurity Anderson-Holstein model is solved by using the exact diagonalization method [3]. Our Hamiltonian is given by

$$H = \sum_{ij\sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + \epsilon_f \sum_{i\sigma} f_{i\sigma}^\dagger f_{i\sigma} + V \sum_{i\sigma} (f_{i\sigma}^\dagger c_{i\sigma} + c_{i\sigma}^\dagger f_{i\sigma}) + U \sum_i n_{fi\uparrow} n_{fi\downarrow} \\ + \omega_0 \sum_i b_i^\dagger b_i + g \sum_i (b_i^\dagger + b_i) \left( \sum_\sigma n_{fi\sigma} - 1 \right),$$

where  $c_{i\sigma}^\dagger$ ,  $f_{i\sigma}^\dagger$  and  $b_i^\dagger$  are creation operators for a conduction ( $c$ )-electron with spin  $\sigma$  at site  $i$ , for a  $f$ -electron and for a phonon, respectively, and  $n_{fi\sigma} = f_{i\sigma}^\dagger f_{i\sigma}$ . The quantities,  $\epsilon_f$ ,  $V$ ,  $U$ ,  $g$  and  $\omega_0$  are the atomic  $f$ -level, the  $c$ - $f$  mixing, the on-site Coulomb interaction, the electron-phonon coupling strength and the phonon frequency, respectively. We assume a semielliptic DOS for the bare conduction band with the half-bandwidth  $W = 1$ .

As shown in Fig.1(a), for the strong electron-phonon coupling  $g \gtrsim g_c$ , the system shows an anomalous heavy-fermion behaviour which is accompanied by a large lattice fluctuation and an extreme phonon softening. We also calculate an effective potential for the ions and find that a simple harmonic potential for  $g \lesssim g_c$  changes into a double-well potential for  $g \gtrsim g_c$  (Fig.1(b)). The effective pairing interaction between the conduction electrons  $\Gamma_c$  has a maximum at  $g \approx g_c$  where the superconducting transition temperature is expected to show a peak (Fig.1(c)).

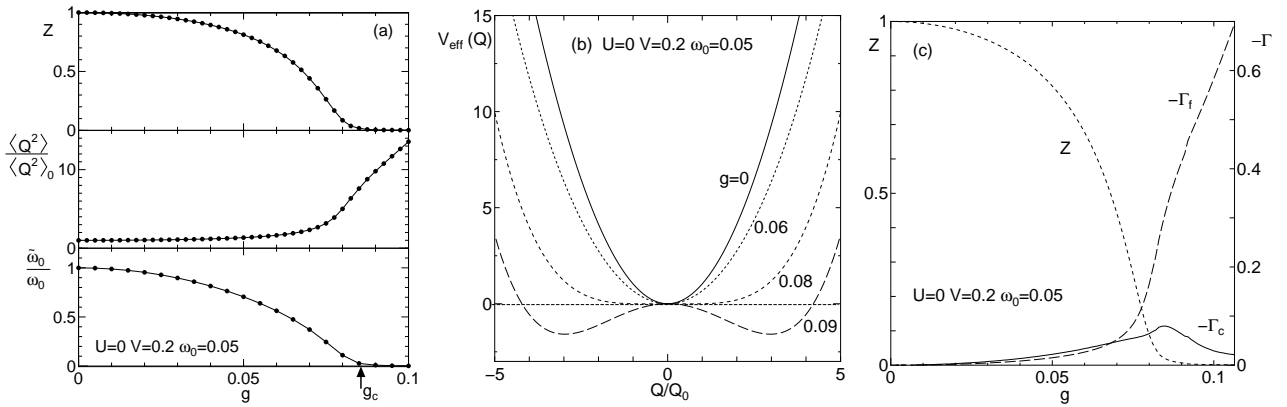


Figure 1: (a) The quasiparticle weight  $Z$  ( $= m/m^*$ ), the lattice fluctuation  $\langle Q^2 \rangle$  and the lowest excited energy of the phonons  $\tilde{\omega}_0$ . (b) The effective potential for the ions  $V_{\text{eff}}(Q)$  for several values of  $g$ . (c) The vertex function for  $f$ -electrons  $\Gamma_f$  and that for  $c$ -electrons  $\Gamma_c$ .

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